

## 1-5 Videos Guide

### 1-5a

- Equations of a line in space parallel to the vector  $\mathbf{v} = \langle a, b, c \rangle$  and containing the point  $(x_0, y_0, z_0)$ 
  - Vector equation:  $\mathbf{r}(t) = \langle x_0, y_0, z_0 \rangle + t\langle a, b, c \rangle$
  - Parametric equations:  $x = x_0 + at, y = y_0 + bt, z = z_0 + ct$
  - Symmetric equations:  $\frac{x-x_0}{a} = \frac{y-y_0}{b} = \frac{z-z_0}{c}$

Exercise:

- Find a vector equation and parametric equations for the line through the point  $(6, -5, 2)$  and parallel to the vector  $\langle 1, 3, -\frac{2}{3} \rangle$ .

### 1-5b

- Vector equation of a line segment from  $P(x_0, y_0, z_0)$  to  $Q(x_1, y_1, z_1)$ :  
Let  $\mathbf{r}_0(t) = \langle x_0, y_0, z_0 \rangle$  and  $\mathbf{r}_1(t) = \langle x_1, y_1, z_1 \rangle$ 
  - $\mathbf{r}(t) = (1-t)\mathbf{r}_0 + t\mathbf{r}_1, \quad 0 \leq t \leq 1$

### 1-5c

- Equation of a plane with normal vector  $\mathbf{n} = \langle a, b, c \rangle$  and containing the point  $(x_0, y_0, z_0)$ 
  - $a(x - x_0) + b(y - y_0) + c(z - z_0) = 0$

Exercises:

- Visually represent the portion of the plane  $3x + 4y + 6z = 12$  that is in the first octant.

### 1-5d

- Find an equation of the plane through the points  $(3, 0, -1)$ ,  $(-2, -2, 3)$ , and  $(7, 1, -4)$ .

### 1-5e

- Find an equation of the plane that passes through the point  $(6, -1, 3)$  and contains the line with symmetric equations  $x/3 = y + 4 = z/2$ .
- Where does the line through  $(-3, 1, 0)$  and  $(-1, 5, 6)$  intersect the plane  $2x + y - z = -2$ ?

### 1-5f

- (a) Find parametric equations for the line of intersection of the planes and (b) find the angle between the planes.  
 $x + y + z = 1, \quad x + 2y + 2z = 1$

### 1-5g

- Distance from a point  $(x_1, y_1, z_1)$  to a plane with equation  $ax + by + cz + d = 0$

$$\circ D = \frac{|ax_1 + by_1 + cz_1 + d|}{\sqrt{a^2 + b^2 + c^2}}$$

Exercises:

- Find the distance from the point  $(-6, 3, 5)$  to the plane  $x - 2y - 4z = 8$ .

1-5h

- Find the distance between the skew lines with the given parametric equations.

$$\begin{array}{lll} x = 1 + t & \text{and} & x = 1 + 2s \\ y = 1 + 6t & & y = 5 + 15s \\ z = 2t & & z = -2 + 6s \end{array}$$